

## Nomenclature (summary for whole course)

USC Viterbi  
School of Engineering

Symbol	Meaning (units)
A	Cross-section area (m <sup>2</sup> )
A*	Throat area (m <sup>2</sup> )
A <sub>e</sub>	Exit area (m <sup>2</sup> )
B	Pre-exponential factor in reaction rate expression (AME 513a) = Z in 513b ([moles/m <sup>3</sup> ] <sup>1-n</sup> K <sup>-n</sup> /s) (n = order of reaction)
B	Transfer number for droplet burning (---)
c	Sound speed (m/s)
C	Duct circumference (m)
C <sub>D</sub>	Drag coefficient (---)
C <sub>f</sub>	Friction coefficient (---)
CO	Carbon monoxide (compound having 1 carbon and 1 oxygen atom)
C <sub>p</sub>	Heat capacity at constant pressure (J/kgK)
C <sub>v</sub>	Heat capacity at constant volume (J/kgK)
D	Mass diffusivity (m <sup>2</sup> /s)
D	Drag force (N)
DORF	Degree Of Reaction Freedom
E	Energy contained by a substance = U + KE + PE (J)
E <sub>a</sub>	Activation Energy (J/mole)

## Nomenclature (summary for whole course)

Symbol	Meaning (units)
f	Fuel mass fraction in mixture (---)
FAR	Fuel to air mass ratio (---)
g	Acceleration of gravity (m/s <sup>2</sup> )
g	Gibbs function = h - Ts (J/kg)
H	Enthalpy = U + PV (J)
h	Enthalpy per unit mass = u + Pv (J/kg)
h	Heat transfer coefficient (usually W/m <sup>2</sup> K, dimensionless in AirCycles.xls files)
$\tilde{h}_i$	Enthalpy of chemical species i per mole = (J/mole)
$[\tilde{h}(T) - \tilde{h}_{298}]_i$	Thermal enthalpy of chemical species i per mole = $(\tilde{h}_{298,i} - \tilde{h}_{298,i}^0) + \int_{298}^T \tilde{c}_{p,i} dT$ (J/mole)
I <sub>SP</sub>	Specific impulse (sec)
K <sub>i</sub>	Equilibrium constant of chemical species i (---)
k	Thermal conductivity (W/mK)
k	Reaction rate constant ([moles/m <sup>3</sup> ] <sup>1-n</sup> /sec) (n = order of reaction)
K	Droplet burning rate constant (m <sup>2</sup> /s)
K	Stretch rate (1/s) (in 513a notation; = Σ in 513b)
Ka	Karlovitz number (= 0.157 Re <sub>L</sub> <sup>-1/2</sup> (u' / S <sub>L</sub> ) <sup>2</sup> for premixed flames in turbulent flows)
KE	Kinetic energy (J or J/kg)
L	Lift force (N)
L <sub>f</sub>	Jet flame length (m)
L <sub>i</sub>	Integral length scale of turbulence (m)
LOMA	Law Of Mass Action

AME 513b - Spring 2020 - Lecture 1 - Introduction

3

## Nomenclature (summary for whole course)

Symbol	Meaning (units)
M <sub>i</sub>	Molecular weight of chemical species i (kg/mole)
M	Mach number (---)
m	mass (kg)
$\dot{m}$	Mass flow rate (kg/sec)
$\dot{m}_a$	Air mass flow rate (kg/s)
$\dot{m}_f$	Fuel mass flow rate (kg/s)
n	Order of reaction (---)
n	Exponent on T term in expression for reaction rate constant k
n <sub>i</sub>	Number of moles of chemical species i
N	Number of chemical species in a mixture
NO	Nitric oxide (compound having 1 nitrogen atom and 1 oxygen atom)
NO <sub>x</sub>	Oxides of Nitrogen (any compound having nitrogen and oxygen atoms)
O <sub>3</sub>	Ozone
P	Pressure (N/m <sup>2</sup> )
P <sub>a</sub>	Ambient pressure (N/m <sup>2</sup> )
P <sub>e</sub>	Exit pressure (N/m <sup>2</sup> )
P <sub>ref</sub>	Reference pressure (101325 N/m <sup>2</sup> )
P <sub>t</sub>	Stagnation pressure (N/m <sup>2</sup> )
PE	Potential Energy (J or J/kg)
$\dot{Q}$	Heat transfer (J or J/kg)
$\dot{Q}$	Heat transfer rate (Watts or Watts/kg)
Q <sub>R</sub>	Fuel heating value (J/kg)

AME 513b - Spring 2020 - Lecture 1 - Introduction

4

## Nomenclature (summary for whole course)

Symbol	Meaning (units)
R	Gas constant = $\mathfrak{R}/M$ (J/kgK)
R	Flight vehicle range (m)
r or $r_c$	Compression ratio = $(V_c+V_d)/V_c$ (---)
$r_e$	Expansion ratio (---)
$Re_L$	Reynolds number of turbulence = $u' L/\nu$ (---)
$\mathfrak{R}$	Universal gas constant = 8.314 J/moleK
S	Entropy (J/K)
s	Entropy per unit mass (J/kgK)
$S_L$	Laminar burning velocity (m/s)
$S_T$	Turbulent burning velocity (m/s)
ST	Specific Thrust
T	Temperature (K)
TSFC	Thrust Specific Fuel Consumption
$T_{ad}$	Adiabatic Flame Temperature (K)
$T_i$	Stagnation temperature (K)
$T_w$	Wall temperature
$T_\infty$	Ambient Temperature (K)

## Nomenclature (summary for whole course)

Symbol	Meaning (units)
U	Internal energy (J)
u	Internal energy per unit mass (J/kg)
u	Velocity (m/s) (most easily confused nomenclature – internal energy vs. velocity)
$u_e$	Exit velocity (m/s)
$u_f$	Flight velocity (m/s)
$u'$	Turbulence intensity (m/s)
UHC	Unburned hydrocarbons
V	Volume ( $m^3$ )
v	Specific volume = $1/\rho$ ( $m^3/kg$ )
W	Work transfer (J or J/kg)
$\dot{W}$	Work transfer rate (Watts or Watts/kg)
$X_f$	Mole fraction fuel in mixture (---)
$X_i$	Mole fraction of chemical species i (---)
$Y_f$	Mass fraction of fuel in mixture (---)
Z	Pre-exponential factor in reaction rate expression (AME 513b) = B in 513a ( $[moles/m^3]^{1-n}K^{-a}/s$ ) (n = order of reaction)
z	Elevation (m)

## Nomenclature (summary for whole course)

Symbol	Meaning (units)
$[ ]_i$	Concentration of species $i$ (moles/m <sup>3</sup> )
$( )^*$	Property at reference state (Mach number = 1 for all cases considered in this course)
$\alpha$	Thermal diffusivity (m <sup>2</sup> /s)
$\beta$	Non-dimensional activation energy $\equiv E/RT$ (---)
$\delta$	Flame thickness (m)
$\Delta \bar{h}_{f,i}^o$	Enthalpy of formation of chemical species $i$ at 298K and 1 atm (J/mole)
$\Delta \bar{s}_i^o(T)$	Entropy of chemical species $i$ at temperature $T$ and 1 atm (J/mole K)
$\phi$	Equivalence ratio (---)
$\gamma$	Gas specific heat ratio $\equiv C_p/C_v$ (---)
$\eta$	Efficiency (thermal efficiency unless otherwise noted)
$\eta_b$	Burner (combustor) efficiency for gas turbine engines (---)
$\eta_d$	Diffuser efficiency for propulsion engines (---)
$\eta_e$	Expansion efficiency for reciprocating engines (---)
$\eta_n$	Nozzle efficiency for propulsion engines (---)
$\eta_o$	Overall efficiency (---)
$\eta_p$	Propulsive efficiency (---)
$\eta_{th}$	Thermal efficiency (---)

## Nomenclature (summary for whole course)

Symbol	Meaning (units)
$\mu$	Dynamic viscosity (kg/m s)
$\nu$	Stoichiometric coefficient (---)
$\nu$	Kinematic viscosity $\equiv \mu/\rho$ (m <sup>2</sup> /s)
$\pi_i$	Stagnation pressure ratio across component $i$ ( $i$ = diffuser (d), burner (b), or nozzle (n))
$\pi_r$	$= P_{1i}/P_1$ ("recovery pressure" ratio) $= \{1 + [(\gamma-1)/2]M^2\}^{\gamma/(\gamma-1)}$ if $\gamma = \text{constant}$
$\rho$	Density (kg/m <sup>3</sup> )
$\Sigma$	Stretch rate (1/s) (= $K$ in 513a notation)
$\tau$	Torque (N m)
$\tau_r$	$= T_{4i}/T_1$ (ratio of maximum allowable turbine inlet temperature to ambient temperature)
$\tau_r$	$= T_{1i}/T_1$ ("recovery temperature" ratio) $= 1 + [(\gamma-1)/2]M^2$ if $\gamma = \text{constant}$
$\omega$	Chemical reaction rate (mole s <sup>-1</sup> m <sup>-3</sup> )



## ***Outline of 1st lecture***

- What do we do with combustion? Who cares?
- World & US energy usage
- Global warming
- Alternatives to combustion engines
- What do we want to know about combustion?
- Types of combustion

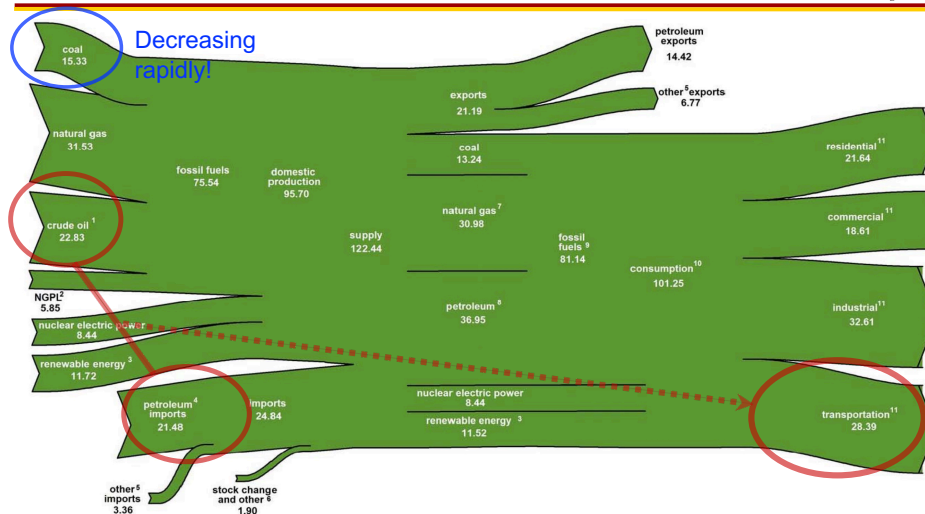
## ***What do we do with combustion?***

- Power generation (coal, natural gas)
- Transportation (land, air, sea vehicles)
- Weapons (rapid production of high-pressure gas)
- Heating
- Lighting
- Cooking (1/3 of the world's population still uses biomass-fueled open fires)
- Hazardous waste & chemical warfare agent destruction
- Production of new materials, e.g. nano-materials
- (Future?) Portable power, e.g. battery replacement
- Unintended / undesired consequences
  - Fires and explosions (residential, urban, wildland, industrial)
  - Pollutants – NO<sub>x</sub> (brown skies, acid rain), CO (poisonous), Unburned HydroCarbons (UHCs, catalyzes production of photochemical smog), formaldehyde, particulates, SO<sub>x</sub>
  - Global warming from CO<sub>2</sub> & other products

## World energy usage

- ≈ 80% of world energy production results from combustion of fossil fuels
- Energy sector accounts for ≈ 10% of US Gross Domestic Product
- Our continuing habit of burning things and our quest to find more things to burn has resulted in
  - Economic booms and busts
  - Political and military conflicts
  - Deification of oil - “the earth’s blood”
  - Global warming (or the need to deny its existence)
  - Human health issues

## US energy flow, 2018, units $10^{15}$ BTU/yr



Each  $10^{15}$  BTU/yr = 1 “Quad”/yr = 33.4 gigawatts

“Renewable energy”: hydroelectric, biomass, geothermal, solar, wind  
[http://www.eia.gov/totalenergy/data/monthly/pdf/flow/total\\_energy.pdf](http://www.eia.gov/totalenergy/data/monthly/pdf/flow/total_energy.pdf)

## US energy demand



2.25 gigawatt coal power plant (Page, AZ), 34% coal-to-electricity efficiency  
 In 2013, Los Angeles DWP received 40% of its electricity from here and a similar plant, but plans to be coal-free by 2025 (most major CA utilities already are)

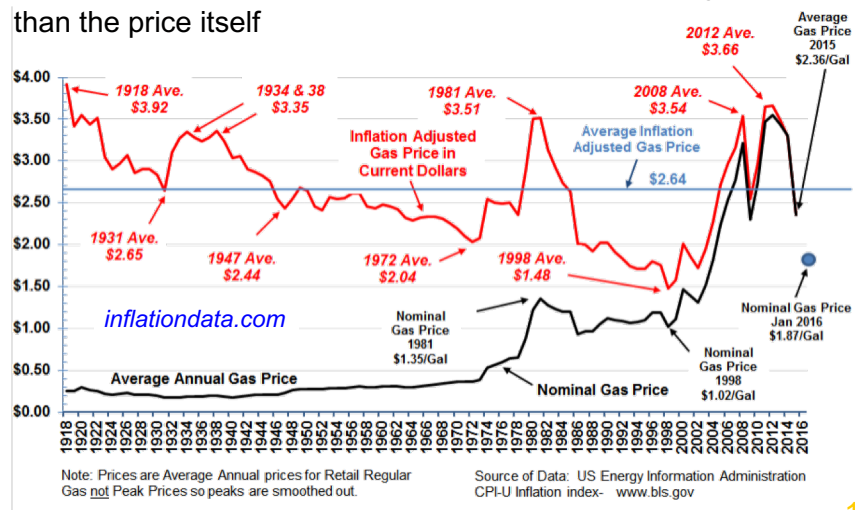
US total energy demand (not just electrical)  $\approx$  500 of these, running continuously 24/7

AME 513b - Spring 2020 - Lecture 1 - Introduction

13

## Inflation-adjusted gasoline prices

- \$2.64/gal  $\pm$  50% for last 100 years
- Even during energy “crises” prices didn’t change that much
- The public is much more sensitive to the rate of change in price than the price itself



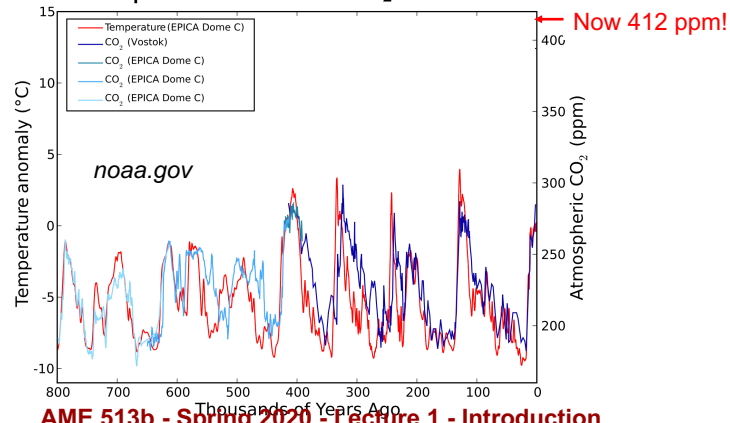
AME 513b - Spring 2020 - Lecture 1 - Introduction

14

## Global warming

- Intergovernmental Panel on Climate Change (> 800 scientists selected from > 3500 nominations) in 2013 <http://www.ipcc.ch/report/ar5/wg1/>

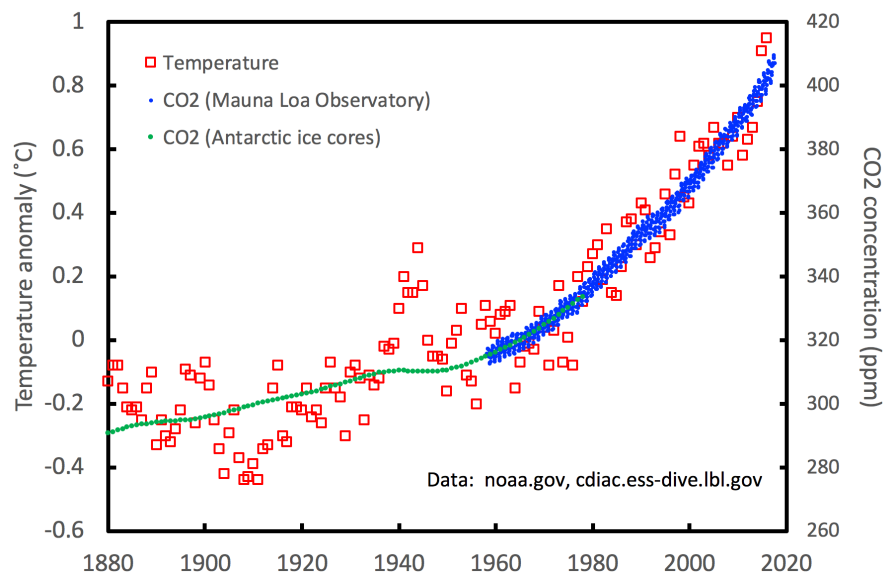
“It is **extremely likely** [>95%] that **more than half** of the observed increase in global average surface temperature from 1951 to 2010 was caused by the anthropogenic increase in greenhouse gas concentrations and other anthropogenic forcings together”



AME 513b - Spring 2020 - Lecture 1 - Introduction

15

## Global warming



AME 513b - Spring 2020 - Lecture 1 - Introduction

16

## Alternatives to Internal Combustion engines USC Viterbi School of Engineering

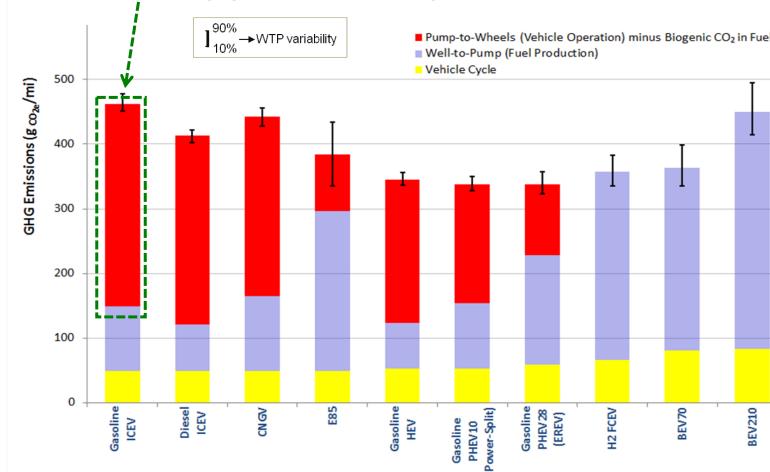
- More information: <http://ronney.usc.edu/AME436/Lecture1>
- No energy technology is without economic and environmental consequences
- Hard to beat liquid-fueled internal combustion engines for
  - Power/weight & power/volume of engine
  - Energy/weight ( $4.3 \times 10^7$  J/kg assuming only fuel, not air, is carried) & energy/volume of liquid hydrocarbon fuel
  - Recharging / refueling rate
  - Low materials cost
    - » ICEs: steel & aluminum
    - » Fuel cells: platinum catalyst, exotic polymer membranes, gold contacts
    - » Batteries: lead, nickel, lithium, gold contacts, ...
  - Distribution & handling convenience of liquids
  - Relative safety of hydrocarbons compared to hydrogen or nuclear energy

AME 513b - Spring 2020 - Lecture 1 - Introduction

17

## Alternatives to Internal Combustion engines USC Viterbi School of Engineering

- Total “cradle to grave” greenhouse gas (GHG) emissions  $\approx$  same for all propulsion methods and energy sources
- Baseline 26.3 mpg gasoline  $\approx$  319 g CO<sub>2</sub>/mi pump-to-wheels



[http://www.hydrogen.energy.gov/pdfs/14006\\_cradle\\_to\\_grave\\_analysis.pdf](http://www.hydrogen.energy.gov/pdfs/14006_cradle_to_grave_analysis.pdf)

AME 513b - Spring 2020 - Lecture 1 - Introduction

18

## ***Practical alternatives...***

- Conservation!
- Aerodynamic, lightweight vehicles (e.g., <http://edison2.com/very-light-car-overview/>)
- Combined cycles
  - Use hot exhaust from ICE to heat water for conventional steam cycle
  - Can achieve > 60% efficiency
  - Not practical for vehicles - too much added volume & weight
- Natural gas (NG)
  - 3.6 cents / kW-hr (electricity 13.3, gasoline 8.0) (latest bls.gov data)
  - Somewhat cleaner than gasoline or diesel, but no environmental silver bullet
  - Low energy storage density when stored as a compressed gas at  $\approx 3000 \text{ lb/in}^2$  - 5x lower than gasoline or diesel
  - Lowest CO<sub>2</sub> emissions of any fossil fuel source
  - Problem: greenhouse effect of unburned NG (escaping from production wells, filling stations, etc.)  $\approx 8x$  that of burned NG

## ***Practical alternatives...***

- Fischer-Tropsch fuels - liquid hydrocarbons from coal or NG
  - Coal or NG + O<sub>2</sub> → CO + H<sub>2</sub> → liquid fuel
  - Competitive with  $\approx$  \$75/barrel oil
  - Cleaner than gasoline or diesel
  - ... but using coal increases greenhouse gases!  
Coal : oil : natural gas  $\approx 2 : 1.5 : 1$
  - Can use biomass (e.g. agricultural waste) instead of coal or natural gas as "energy feedstock"

## Why do we need to study combustion?

- Chemical thermodynamics only tells us the **end states** - what happens if we wait “forever and a day” for chemical reaction to occur
- We need to know **how fast** reactions occur
  - How fast depends on both the inherent rates of reaction and the rates of heat and mass transport to the reaction zone(s)
  - Chemical reactions + heat & mass transport = **combustion**
  - Some reactions occur too slowly to be observed, e.g.  
 $2 \text{NO} \rightarrow \text{N}_2 + \text{O}_2$   
has an adiabatic flame temperature of 2650K but no one has ever made a flame with NO because reaction rates are too slow!
- Chemical reaction leads to gradients in temperature, pressure and species concentration
  - Results in transport of energy, momentum, mass
- Combustion is the study of the coupling between **thermodynamics, chemical reaction** and **transport processes**

## What do we want to know about combustion?

- From combustion device
  - Power (thermal, electrical, shaft, propulsive)
  - Efficiency (% fuel burned, % fuel converted to shaft, electrical and/or propulsive power)
  - Emissions
- From combustion process itself
  - Rates of consumption
    - » Reactants
    - » Intermediates
  - Rates of formation
    - » Intermediates
    - » Products
  - Global properties
    - » Rates of flame propagation
    - » Rates of heat generation (more precisely, rate of conversion of chemical enthalpy to thermal enthalpy)
    - » Temperatures
    - » Pressures

## Types of combustion

- **Premixed** - reactants are intimately mixed on the molecular scale before combustion is initiated; several flavors
  - Deflagration
  - Detonation
  - Homogeneous reaction
- **Nonpremixed** - reactants mix only at the time of combustion - have to **mix** first then **burn**; several flavors
  - Gas jet (Bic lighter)
  - Liquid fuel droplet
  - Liquid fuel jet (e.g. Kuwait oil fire, candle, Diesel engine)
  - Solid (e.g. coal particle, wood)

Type	Chemical reaction	Heat / mass transport	Momentum transport	Thermodynamics
Deflagration			X	
Detonation	X	X		
Homogeneous reaction		X	X	
Nonpremixed flames	X		X	X

AME 513b - Spring 2020 - Lecture 1 - Introduction

23

## Deflagrations

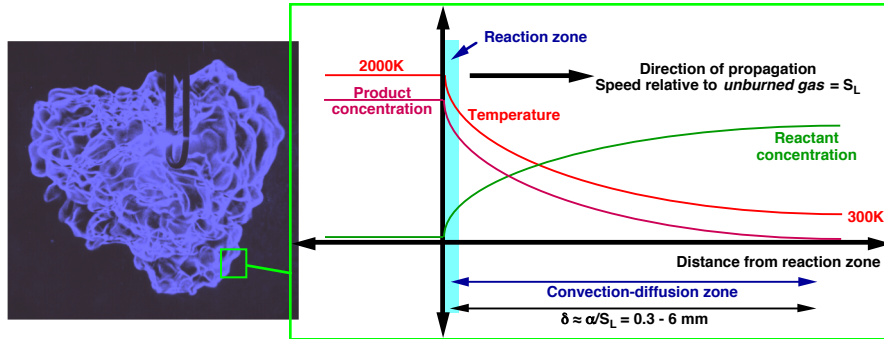
- **Subsonic propagating** front sustained by conduction of heat from the hot (burned) gases to the cold (unburned) gases which raises the temperature enough that chemical reaction can occur; since chemical reaction rates are very sensitive to temperature, most of the reaction is concentrated in a thin zone near the high-temperature side
- May be laminar or turbulent
- Temperature increases in “convection-diffusion zone” or “preheat zone” ahead of reaction zone, even though no heat release occurs there, due to balance between convection & diffusion
- Reactant concentration decreases in convection-diffusion zone, even though no chemical reaction occurs there, for the same reason
- How can we have reaction at the reaction zone even though reactant concentration is low there? (See diagram...) Because reaction rate is much more sensitive to temperature than reactant concentration, so benefit of high T outweighs penalty of low concentration

AME 513b - Spring 2020 - Lecture 1 - Introduction

24



## Schematic of deflagration

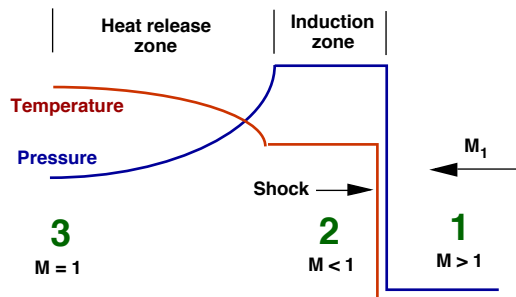


Turbulent premixed flame experiment in a fan-stirred chamber (<http://www.mech-eng.leeds.ac.uk/res-group/combustion/activities/Bomb.htm>)

Flame thickness ( $\delta$ )  $\sim \alpha/S_L$   
( $\alpha$  = thermal diffusivity)

## Premixed flames - detonation

- **Supersonic** propagating front sustained by heating via shock wave
  - After shock front, need time (thus distance = time x velocity) before reaction starts to occur (“induction zone”)
  - After induction zone, chemical reaction & heat release occur
  - Pressure & temperature behavior coupled strongly with supersonic/subsonic gasdynamics
  - Ideally only  $M_3 = 1$  “Chapman-Jouget detonation” is stable  
( $M$  = Mach number =  $u/c$ ;  $u$  = velocity,  
 $c$  = sound speed =  $(\gamma RT)^{1/2}$  for ideal gas)



CJ detonation :

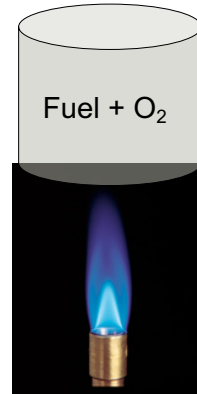
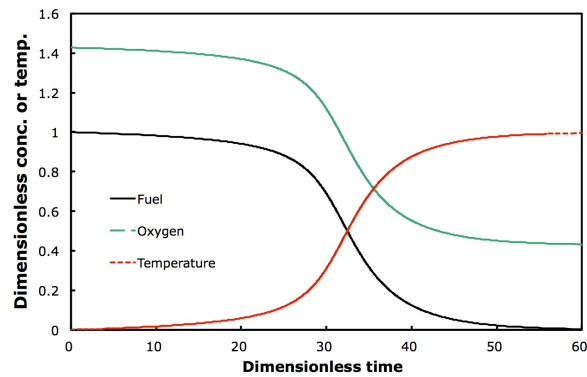
$$M_1 = \left[ 1 + \frac{H(\gamma^2 - 1)}{2\gamma} \right]^{1/2} + \left[ \frac{H(\gamma^2 - 1)}{2\gamma} \right]^{1/2}$$

$$H = \frac{q}{RT_1} \text{ (heat release parameter)}$$

$$q = C_p(T_{3t} - T_{2t}) = fQ_R$$

## Premixed flames - homogeneous reaction USC Viterbi School of Engineering

- Model for knock in premixed-charge engines
- Fixed mass with uniform (in space) T, P, composition
- No "propagation" in space but propagation in time
- In laboratory, could heat chamber to a certain T and measure time to react; in engine, compression of mixture (increases P & T, thus reaction rate) initiates reaction



AME 513b - Spring 2020 - Lecture 1 - Introduction

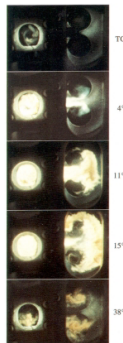
27

## "Non-premixed" or "diffusion" flames USC Viterbi School of Engineering

- Reaction zone where fuel & O<sub>2</sub> fluxes in stoichiometric proportion
- Generally "mixed is burned" - mixing slower than chemical reaction
- No inherent propagation rate (flame location determined by stoichiometric location)
- No inherent thickness ( $\delta = \text{mixing layer thickness} \sim (\alpha/\Sigma)^{1/2}$ ) ( $\Sigma = \text{stretch rate}$ )
- Unlike premixed flames with characteristic propagation rate  $S_L$  and thickness  $\delta \sim \alpha/S_L$  that are almost independent of  $\Sigma$



Candle  
Diesel engine



Kuwait  
Oil fire

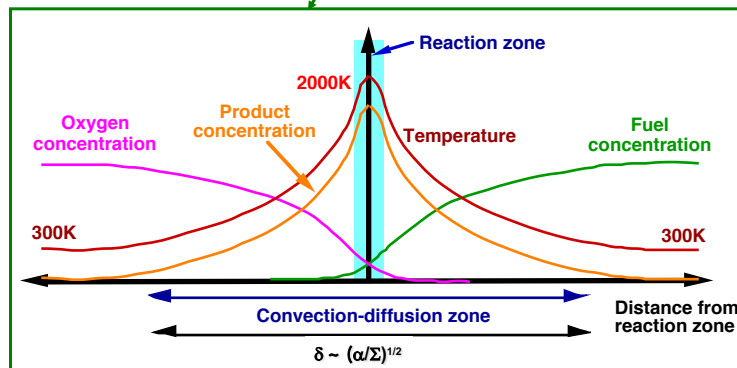
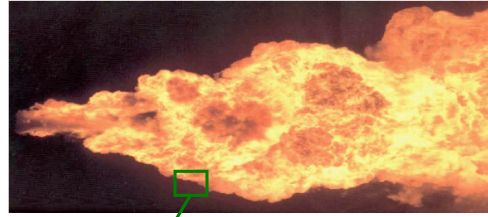


Forest fire

AME 513b - Spring 2020 - Lecture 1 - Introduction

28

## Nonpremixed flame structure

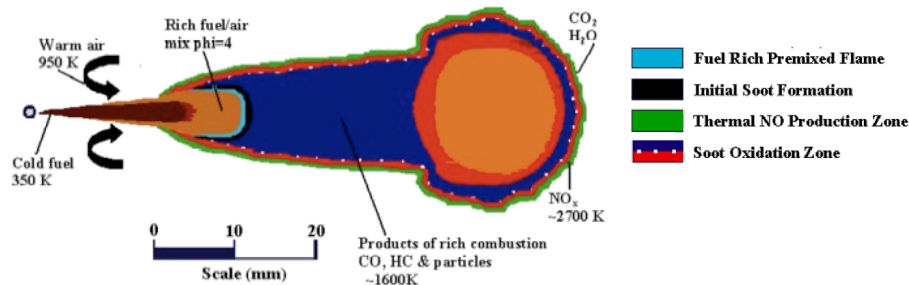


AME 513b - Spring 2020 - Lecture 1 - Introduction

29

## Diesel engine combustion

- Two extremes in practical combustors
  - Droplet combustion - vaporization of droplets is slow, so droplets burn as individuals
  - Gas-jet flame - vaporization of droplets is so fast, there is effectively a jet of fuel vapor rather than individual droplets
  - Reality is in between, but in Diesel combustion usually closer to the gas jet “with extras” – regions of premixed combustion



Flynn, P.F, R.P. Durrett, G.L. Hunter, A.O. zur Loye, O.C. Akinyemi, J.E. Dec, C.K. Westbrook, SAE Paper No. 1999-01-0509.

AME 513b - Spring 2020 - Lecture 1 - Introduction

30

## Summary - Lecture 1

- Combustion is the interaction of thermodynamics, chemical reaction and heat/mass/momentum transport, but which is/are most important depends on the situation
- Combustion is ubiquitous in our everyday lives and will continue to be for our lifetimes
- Many advantages of fossil fuels over other energy sources
  - Cheap (?), plentiful (?), clean (?)
  - Energy/weight of fuel itself
  - Power/weight of engines
  - Materials costs of combustion engines (*e.g.*, compared to fuel cells)
- The most important distinction between flames is premixed vs. non-premixed, *i.e.*, whether the reactants are mixed before combustion

## Discussion point

Our current energy economy, based primarily on fossil fuel usage, evolved because it was the cheapest system. Is it possible that it's also the most environmentally responsible (or "least environmentally irresponsible") system?