

Outline

USC Viterbi
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- AirCyclesForRecips.xls spreadsheet - how it works and how to use it
- Some non-ideal effects
 - Irreversible compression/expansion
 - Heat transfer to gas during cycle
 - Finite burn time / spark advance
 - Exhaust residual
 - Friction
- Factors that limit maximum RPM
- Performance plots - Power & Torque vs. RPM

- Thermodynamic model is **exact**, but heat loss, burn rate, etc. models are **qualitative**
- Constant γ not realistic (changes from ≈ 1.4 to 1.25 during the cycle) but only affects results quantitatively (not qualitatively) (1 of 2 most significant weaknesses of AirCycles4Recips.xls)
- Heat transfer model
 - $\Delta T \sim h(T_{\text{wall}} - T_{\text{gas}})$, where dimensionless heat transfer coefficient (**h**) & cylinder wall temperature (T_{wall}) are specified constants - physically reasonable
 - **h** is a "Sherwood number" = $h/\rho C_p L N$, where h is the dimensional heat transfer coefficient ($\text{W}/\text{m}^2\text{K}$) and L is a characteristic dimension (e.g. cylinder diameter) (LN is a characteristic velocity; if L = stroke then LN = mean piston speed)
 - Increments each cell not each time step
 - Doesn't include effects of varying area, varying turbulence, varying time scale through piston motion, etc. on **h**

- Work transfer from step i to step $i+1$
 - $\delta W = \delta Q - dU$ (1st Law of Thermo, conservation of energy)
 - $\delta Q = C_v h(T_{\text{wall}} - T_i) + (\Delta f) Q_R / C_v$
 - $dU = U_{i+1} - U_i = C_v (T_{i+1} - T_i)$ (constant C_v)
 - Δf = increment of fuel burned in current step
- Friction loss is a specified FMEP
- Use latest version from AME 436 website - some plots embedded in lecture notes were built with earlier versions
- Model considers only 1 gas in cylinder - improved model should consider 2 separate gases, burned & unburned, with combustion increasing amount of burned gas (2nd significant weakness of AirCycles4Recips.xls)

AirCycles4Recips.xls - intake process

- Intake process spread across 25 Excel cells ($i = 1, 2, \dots, 25$); 1/25 of total cylinder volume increase in each successive cell
- Pressure P_{intake} & specific volume v_{intake} assumed constant
- In first row of intake process
 - If "Exhaust Residual" = FALSE then $T = T_{\text{intake}}$
 - If "Exhaust Residual" = TRUE then T = final exhaust temperature after expansion, blowdown, and intake start
- If "Exhaust residual" = TRUE, iteration required since the exhaust temperature is not known until the end of the cycle; use SOLVE button to update solution after changing any input parameter (otherwise SOLVE button does nothing)
- After first row $T_{\text{intake}} = T$ of the fresh gas but it mixes with gas already in cylinder that has different T due to heat loss /gain; mixed gas T conserves internal energy of fresh + existing charge:

$$(m_{i+1})C_v T_{i+1} = m_i C_v T_i + \Delta m C_v T_{\text{intake}}$$

where $\Delta m = m_{i+1} - m_i = (V_{i+1} - V_i) / v_{\text{intake}} = (V_{i+1} - V_i) / (RT_{\text{intake}} / P_{\text{intake}})$

AirCycles4Recips.xls - compression

- Compression spread across 25 cells; 1/25 of total cylinder volume decrease in each successive cell
- Done in two steps:
 - (1) Wall heat transfer at constant volume

$$T_{i,b} = T_{i,a} + h(T_w - T_{i,a}); v_{i,b} = v_{i,a}$$
 - (2) Adiabatic compression according to the usual PV^γ relations; may be irreversible according to (see lecture 7, pages 17-18)

$$\eta_{\text{comp}} \equiv \frac{(v_i / v_{i+1})^{\gamma-1} - 1}{T_{i+1,a} / T_{i,b} - 1} \Rightarrow T_{i+1,a} = T_{i,b} \left(1 + \frac{(v_i / v_{i+1})^{\gamma-1} - 1}{\eta_{\text{comp}}} \right)$$

$\eta_{\text{comp}} = 1 \Rightarrow$ reversible adiabatic process
- Compression ends at volume $V_c + V_d * \text{BurnStart}$, where BurnStart is a specified number ($0 \leq \text{BurnStart} < 1$)
- BurnStart must be ≥ 0 , i.e. combustion must start at or before minimum volume (a limitation of the spreadsheet, not a fundamental limitation of cycles)
- If BurnStart > 0 , some compression occurs during heat addition step (next...)

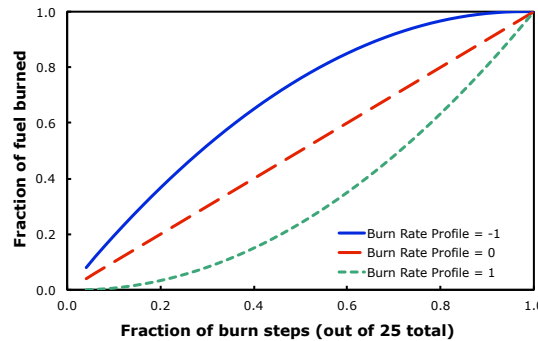
AirCycles4Recips.xls - combustion

- Same two-step process of heat transfer at constant V + adiabatic compression, but now **both heat transfer to/from wall AND heat input due to combustion**

$$T_{i,b} = T_{i,a} + h(T_w - T_{i,a}) + (\Delta f)Q_R / C_v; v_{i,b} = v_{i,a}$$

Δf = fraction of fuel burned during step

- By default (Burn Rate Profile = 0) $\Delta f = f/25$, but can use Burn Rate Profile > 0 or < 0 to have more burning near end (realistic) or beginning (unrealistic) of combustion process



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AirCycles4Recips.xls - combustion

- If BurnStart > 0 then compression continues (with combustion) until minimum cylinder volume (= V_c)
- Heat addition ends at volume $V_c + V_d * \text{BurnEnd}$, where BurnEnd is specified ($0 \leq \text{BurnEnd} < 1$)
- Note two stages of heat addition corresponding to volumes:
 - (1) $V_c + V_d * \text{BurnStart} \rightarrow V_c$
 - (2) $V_c \rightarrow V_c + V_d * \text{BurnEnd}$
- If BurnEnd > 0, expansion occurs in conjunction with heat addition
- As with BurnStart, BurnEnd must be ≥ 0 , i.e. combustion must end at or after minimum cylinder volume
- If "Const V comb?" = FALSE, constant **pressure** combustion is calculated (Diesel cycle); BurnStart, BurnEnd, BurnRateProfile have no effect and

$$T_{i,b} = T_{i,a} + h(T_w - T_{i,a}) + (\Delta f)Q_R / C_p; v_{i,b} = v_{i,a} (T_{i,b} / T_{i,a})$$

(Same as before but with C_p instead of C_v , and volume (v) increasing rather than constant)

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Expansion process

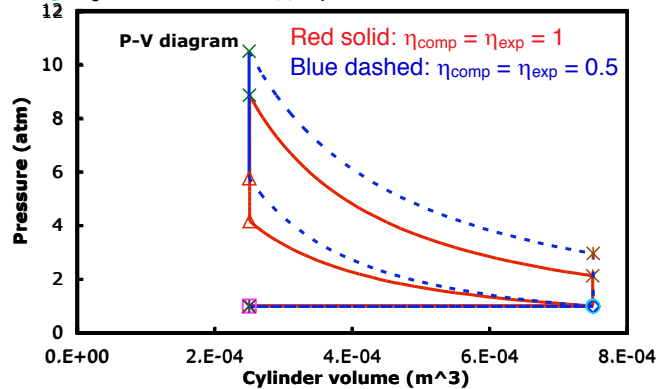
- **Expansion** spread across 25 cells; 1/25 of total cylinder volume increase in each successive cell
- Done in two steps
 - (1) Wall heat transfer at constant V as usual
 - (2) Adiabatic expansion according to the usual PV^γ relations but may be irreversible according to
$$\eta_{\text{exp}} \equiv \frac{T_{i+1,a}/T_{i,b} - 1}{(v_i/v_{i+1})^{\gamma-1} - 1} \Rightarrow T_{i+1,a} = T_{i,b} \left(1 + \eta_{\text{exp}} \left[(v_i/v_{i+1})^{\gamma-1} - 1 \right] \right)$$
- Followed by expansion to $P = P_{\text{exhaust}} = P_{\text{ambient}}$ if "Complete Expansion" = TRUE; same heat transfer & expansion laws apply

Blowdown, exhaust processes

- "**Blowdown**" or "**blowup**" is assumed isentropic, infinitely fast so no heat transfer; not applicable if complete expansion (already at ambient pressure)
- **Exhaust** process
 - Spread across 25 cells; 1/25 of total cylinder volume decrease in each successive cell
 - P_{exhaust} assumed constant
 - Heat transfer may occur as usual (exhaust heat transfer only affects cycle performance if "Exhaust Residual" = TRUE)

Irreversible (but adiabatic) comp / exp

- If piston expands infinitely fast, no work done (piston outruns gas molecules), no work done; if piston compresses too fast, builds up shocks
- Not important except at very high RPM (choking at valves), important for propulsion at M^2 close to or larger than 1
- P-V diagram - for same ΔV , more ΔP during compression



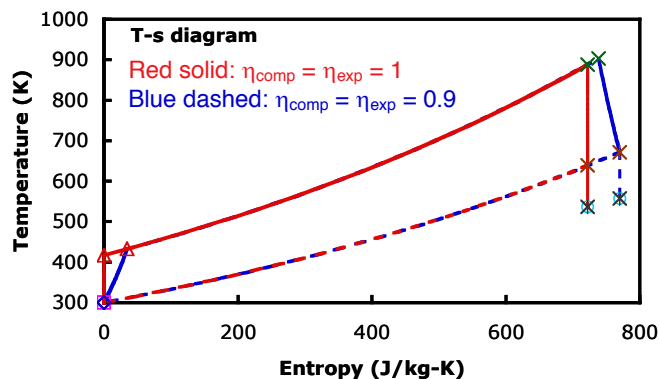
$r = 3, \gamma = 1.3, f = 0.01, Q_R = 4.5 \times 10^7 \text{ J/kg}, T_{in} = 300\text{K}, P_{in} = 1 \text{ atm}, P_{exh} = 1 \text{ atm}.$
 $ExhRes = \text{FALSE}, \text{Const-v comb} = \text{TRUE}, \text{BurnStart} = \text{BurnEnd} = \text{BurnRateProfile} = 0,$
 $ComplExp = \text{FALSE}, h = 0, \eta_{comp} = \eta_{exp} = 0.5 \text{ or } 1$

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Irreversible (but adiabatic) comp / exp

- Larger change in T-s diagram - for same ΔV , more ΔT (\Rightarrow more work) during compression, less ΔT (\Rightarrow less work) during expansion since $\Delta s > 0$ with irreversible compression/expansion (see lecture 6)
- Significant effect on $\eta_{th} = 0.281$ ($\eta_{comp} = \eta_{exp} = 1$) vs. 0.211 ($\eta_{comp} = \eta_{exp} = 0.9$) for case shown (note I used $\eta_{comp} = \eta_{exp} = 0.5$ for P-V diagram)



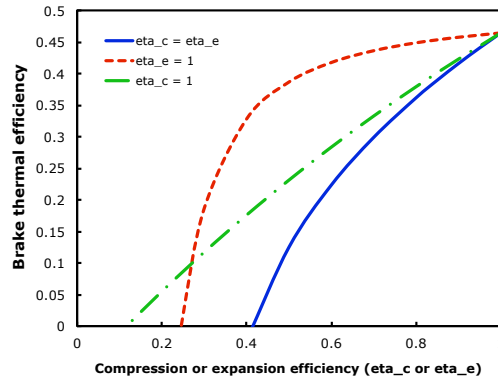
$r = 3, \gamma = 1.3, f = 0.01, Q_R = 4.5 \times 10^7 \text{ J/kg}, T_{in} = 300\text{K}, P_{in} = 1 \text{ atm}, P_{exh} = 1 \text{ atm}.$
 $ExhRes = \text{FALSE}, \text{Const-v comb} = \text{TRUE}, \text{BurnStart} = \text{BurnEnd} = \text{BurnRateProfile} = 0,$
 $ComplExp = \text{FALSE}, h = 0, \eta_{comp} = \eta_{exp} = 0.9 \text{ or } 1$

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Irreversible (but adiabatic) comp / exp

- Moderate irreversibility in compression doesn't hurt much (just a little more compression work) but irreversibility in expansion directly deducts from net work; though severe compression irreversibility hurts more
- (Obviously) combined compression & expansion irreversibility is worst



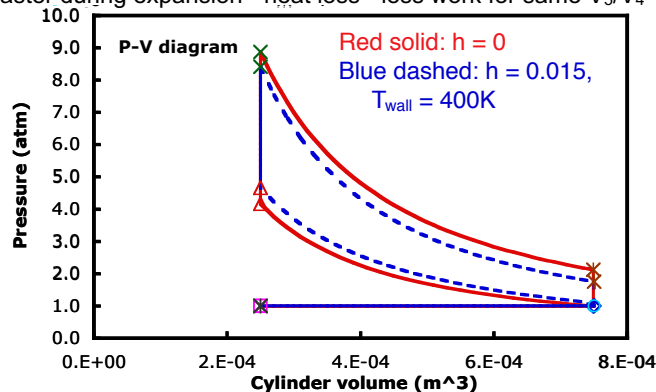
$r = 8$, $\gamma = 1.3$, $f = 0.068$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm.
ExhRes = FALSE, Const-v comb = TRUE, BurnStart = BurnEnd = BurnRateProfile = 0,
ComplExp = FALSE, $h = 0$, $\eta_{comp} = \text{variable}$, $\eta_{exp} = \text{variable}$

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Heat transfer during cycle

- More ΔP during compression - T higher due to heat transfer in - more work required to compress higher- T gas for same V_3/V_2
 $w = mC_v(T_2 - T_3) = mC_vT_2(1 - T_3/T_2) = mC_vT_2[1 - (V_2/V_3)^{\gamma-1}]$
- Less ΔP during combustion - heat loss decreases ΔT thus ΔP for fixed V
- P falls faster during expansion - heat loss - less work for same V_5/V_4



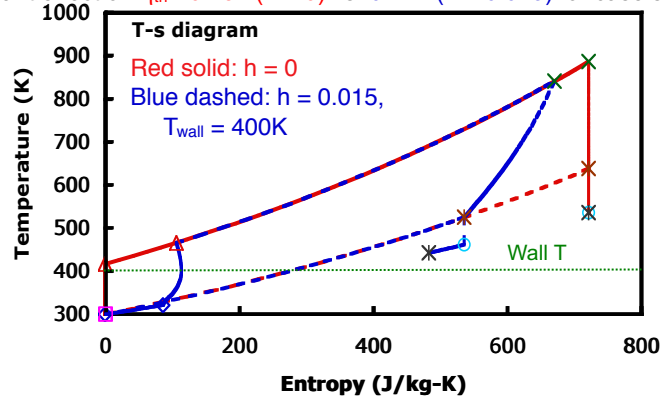
$r = 3$, $\gamma = 1.3$, $f = 0.01$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm
ExhRes = FALSE, Const-v comb = TRUE, BurnStart = BurnEnd = BurnRateProfile = 0
ComplExp = FALSE, $h = 0$ or 0.015 , $T_{wall} = 400$ K, $\eta_{comp} = \eta_{exp} = 1$

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Heat transfer during cycle

- Const. P heat addition during intake, so higher T & s than adiabatic cycle
- Heat addition during 1st part of compression (ds > 0), heat loss (ds < 0) during 2nd part of compression & rest of cycle
- Still const. V combust., so same const.-v curve but less ΔT due to heat loss
- Significant effect on η_{th} - 0.281 (h = 0) vs. 0.177 (h = 0.015) for case shown



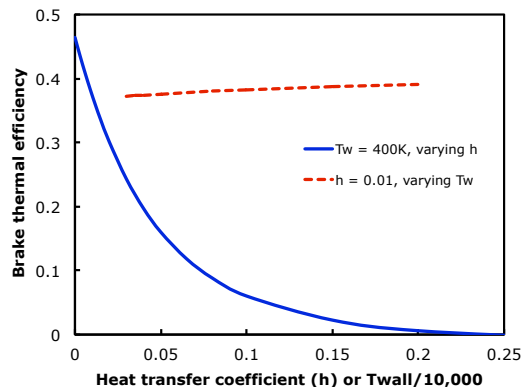
$r = 3$, $\gamma = 1.3$, $f = 0.01$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300K$, $P_{in} = 1$ atm, $P_{exh} = 1$ atm
 ExhRes = FALSE, Const-v comb = TRUE, BurnStart = BurnEnd = BurnRateProfile = 0
 ComplExp = FALSE, h = 0 or 0.015, $T_{wall} = 400K$, $\eta_{comp} = \eta_{exp} = 1$

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Heat transfer during cycle

- Obviously, increasing heat loss coefficient h decreases η_{th}
- Wall T has almost no effect for fixed h - extra heat transfer in during compression (thus more work in) at high T is balanced by more heat transfer during expansion (thus more work out)



$r = 8$, $\gamma = 1.3$, $f = 0.068$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300K$, $P_{in} = 1$ atm, $P_{exh} = 1$ atm
 ExhRes = FALSE, Const-v comb = TRUE, BurnStart = BurnEnd = BurnRateProfile = 0
 ComplExp = FALSE, h = variable, $T_{wall} =$ variable, $\eta_{comp} = \eta_{exp} = 1$

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Heat transfer scaling estimate

- Heat transfer (Q) to a wall at temperature T_w from a slab of gas of thickness Δx , area A & temperature T_g (initially at $T_{g,ad}$)

$$Q = kA(\Delta T/\Delta x) = kA((T_g - T_w)/\Delta x)$$

- Rate of decrease of enthalpy of said slab

$$Q = mC_P(\Delta T/\Delta t) = \rho VC_P((T_{g,ad} - T_g)/\Delta t) = \rho A \Delta x C_P (T_{g,ad} - T_g)/\Delta t$$

- Equate: $(k/\rho C_P)(T_g - T_w)/(T_{g,ad} - T_g) = \alpha(T_g - T_w)/(T_{g,ad} - T_g) = (\Delta x)^2/\Delta t$ or

"Importance of heat losses" $\sim (T_{g,ad} - T_g)/(T_g - T_w) \sim \alpha \Delta t / (\Delta x)^2$

- For turbulent flow, $\alpha \sim u' L_I$
- In an engine, $u' \sim u_{piston} \sim SN$ (S = stroke $\sim \Delta x$, N = RPM),
 $L_I \sim S \sim \Delta x$, $\Delta t \sim 1/N$
- Combining these, $(T_g - T_w)/(T_g - T_\infty) \sim$ constant (independent of engine size (Δx) and rotation rate (N))
- If not turbulent (very low Re , i.e. very low speed or very small engine), $\alpha \approx$ constant (not a function of u' and L_I) then

"Importance of heat losses" $\sim \alpha/NS^2$

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Heat transfer - mini-catechism

- Why do we have heat loss in engines?

Because the cylinder wall is "cold" - typically just a little higher than the cooling water temperature, $\approx 120^\circ\text{C}$ (boiling point at 2 atm). This is much colder than the gases during combustion (2400K) and during expansion (down to 1200K).

- Why do we need to cool the cylinder?

To keep the lubricating oil from getting too hot and breaking down. Also, with too large a temperature increase, thermal expansion will change the fit between the piston and cylinder and make it too tight or too loose.

- How significant is the loss?

See Heywood Fig. 12-4: At low vehicle speed (meaning: low engine RPM, low P_{intake}) 50% of fuel energy is dissipated as cooling system losses; at higher speed, 30%; Heywood (p. 851) states that a 10% decrease in heat loss would mean about 3% increase in BMEP

- Could we reduce the loss by using a ceramic (or whatever material) engine that could withstand high temperatures without oil lubrication?

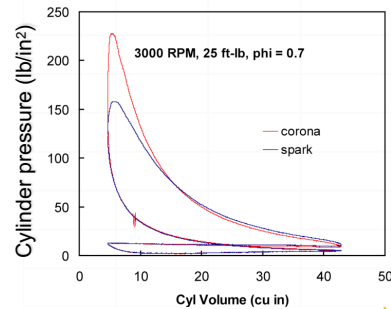
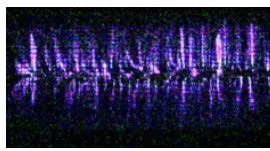
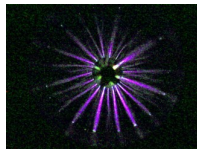
The analysis 2 pages back shows that raising T_{wall} doesn't increase efficiency; what is needed is a more nearly adiabatic engine (lower h). This is borne out by many experiments, peaking in the 1980's, using so-called "adiabatic" or "low heat rejection" engines made of ceramics. This raised T_{wall} but caused more heat transfer during compression, thereby increasing compression work, so the efficiency didn't improve.

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Heat transfer - mini-catechism

- How can we decrease h ?
Heat transfer in engines is controlled by turbulence, so you need to decrease turbulence
- How can you do that?
Engines are designed for high turbulence, so you could reverse-engineer the engine for lower turbulence (e.g. by avoiding swirl in the intake ports, using "anti-squish" (see lecture 4), etc.)
- Why don't we do that now?
Because we need high turbulence (high u') to get fast burning
- Is there any way to burn fast without turbulence?
I'm working on that; one possibility is [transient plasma ignition](#), which produces multiple streamers of electrons, thus multiple ignition sites, for one set of electrodes

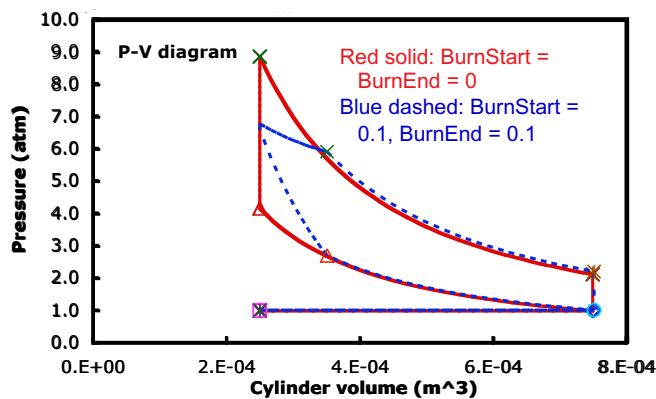


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Slow burn

- For ignition before the minimum volume (**B**efore **T**op **D**ead **C**enter, **BTDC**), P increases faster (since both compression AND burning), but same minimum volume must be reached
- Burning **A**fter **T**op **D**ead **C**enter (**ATDC**) leads to much lower peak P (some burning during expansion) but somewhat higher P during expansion



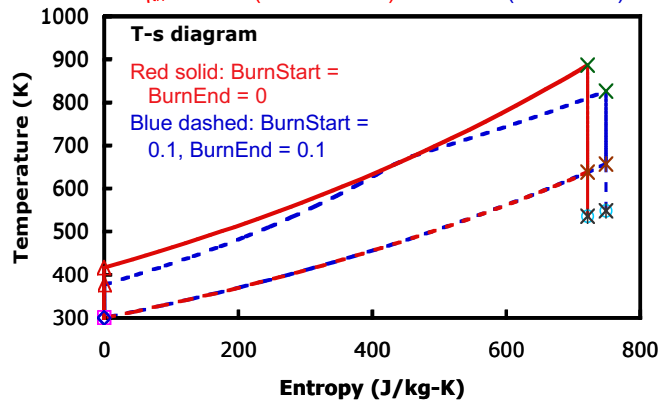
$r = 3$, $\gamma = 1.3$, $f = 0.01$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm, BurnRateProfile = 1, ExhRes = FALSE, Const-v comb = TRUE, ComplExp = FALSE, $h = 0$, $T_{wall} = 400$ K, $\eta_{comp} = \eta_{exp} = 1$

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Slow burn

- Burn starts earlier in compression process, has to go to same v , result is higher s to get same heat addition ($= \int T ds$)
- Difference in work: 2 triangular slivers vs. rectangle
- Burning BTDC or ATDC ALWAYS leads to lower efficiency since ALWAYS lower T_H for same T_L , thus ALWAYS lower efficiency Carnot "strips"
- Moderate effect on η_{th} - 0.281 (Instant burn) vs. 0.242 (slow burn) for case shown



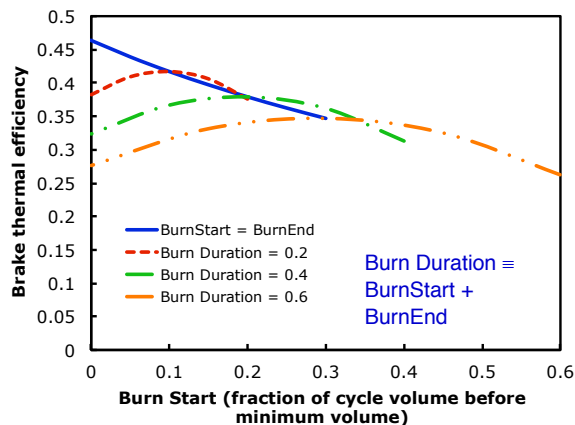
$r = 3$, $\gamma = 1.3$, $f = 0.01$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm, $BurnRateProfile = 1$, $ExhRes = FALSE$, $Const-v\ comb = TRUE$, $ComplExp = FALSE$, $h = 0$, $T_{wall} = 400$ K, $\eta_{comp} = \eta_{exp} = 1$

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Slow burn – impact on ideal cycle

- How to minimize impact of slow burn? Ignite the mixture BTDC; while this means some mixture is burned too early, and some burns ATDC, η_{th} better than if you wait until TDC to start burning



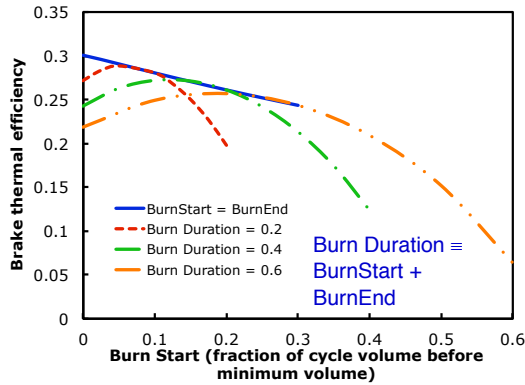
$r = 8$, $\gamma = 1.3$, $f = 0.068$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm, $ExhRes = FALSE$, $Const-v\ comb = TRUE$, $BurnStart = variable$, $BurnEnd = variable$, $BurnRateProfile = 0$, $ComplExp = FALSE$, $h = 0$, $\eta_{comp} = \eta_{exp} = 1$

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Slow burn – impact on non-ideal cycle

- With ideal cycle (no heat losses, reversible compression & expansion, no exhaust residual) optimal timing \approx symmetric (BurnStart = BurnEnd), (previous page), but with non-ideal cycle (below), better to start burning slightly later in cycle (less heat losses)



$r = 8, \gamma = 1.3, f = 0.068, Q_R = 4.5 \times 10^7 \text{ J/kg}, T_{in} = 300\text{K}, P_{in} = 1 \text{ atm}, P_{exh} = 1 \text{ atm}$
 BurnRateProfile = 0, ExhRes = TRUE, Const-v comb = TRUE
 ComplExp = FALSE, $h = 0.01, \eta_{comp} = \eta_{exp} = 0.9$

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Slow burn

- Rule of thumb: best efficiency when ignition timing chosen so that maximum P occurs $\approx 10^\circ$ ATDC
- This spreadsheet: for Burn Duration = 0.15, optimal "timing" is BurnStart = 0.045, BurnEnd = 0.105, more burning ATDC - consistent with real engine
- Leaner mixtures: slower burning, need to advance spark more
- Spark advance sounds good BUT...
 - Peak temperature substantially affected - this affects NO_x formation greatly - high activation energy (E) and knock (next lecture ...)
 - Minimum peak T when BurnStart < BurnEnd, so that more burning occurs AFTER minimum volume
 - "Compress then burn" leads to lower T than "burn then compress" - burn ADDS to T, compression MULTIPLIES T
 - If 1 - 2 is compress, 2 - 3 is burn then

$$T_2 = T_1 r^{\gamma-1}; T_3 = T_2 + fQ_R/C_v = T_1 r^{\gamma-1} + fQ_R/C_v$$
 - If 1 - 2 is burn, 2 - 3 is compress then

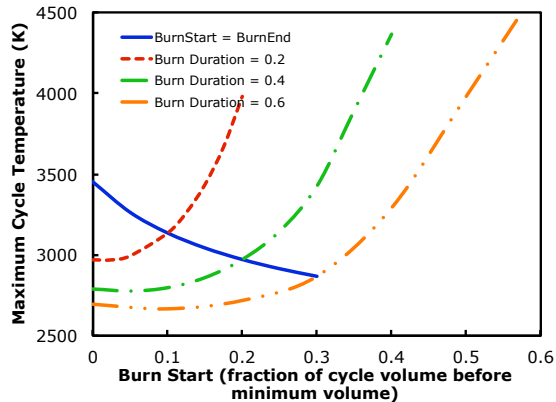
$$T_2 = T_1 + fQ_R/C_v; T_3 = T_2 r^{\gamma-1} = (T_1 + fQ_R/C_v) r^{\gamma-1}$$
 - $T_{3(\text{BurnComb})} - T_{3(\text{CompBurn})} = (fQ_R/C_v)(r^{\gamma-1} - 1) > 0$

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Slow burn - effect on peak cycle T

- As ignition timing is "advanced" (more burning BTDC, moving to right on plot below), peak cycle T increases substantially
- Temperatures are unrealistically high since model assumes constant C_p & C_v , no dissociation but the trend will be the same with "real" gases



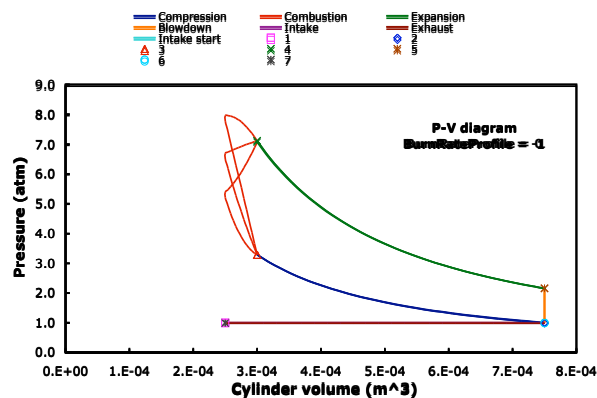
$r = 3$, $\gamma = 1.3$, $f = 0.068$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm
ExhRes = TRUE, Const-v comb = TRUE, BurnStart = variable, BurnEnd = variable
BurnRateProfile = 0, ComplExp = FALSE, $h = 0.01$, $\eta_{comp} = \eta_{exp} = 0.9$

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Burn Rate Profile

- For more burning at beginning of cycle (BurnRateProfile = -1), more "burn then compress," higher peak pressures
- BurnRateProfile > 0 is more realistic since more mass burned late in cycle after pressure (thus density) is higher (S_L & S_T not affected much by pressure)



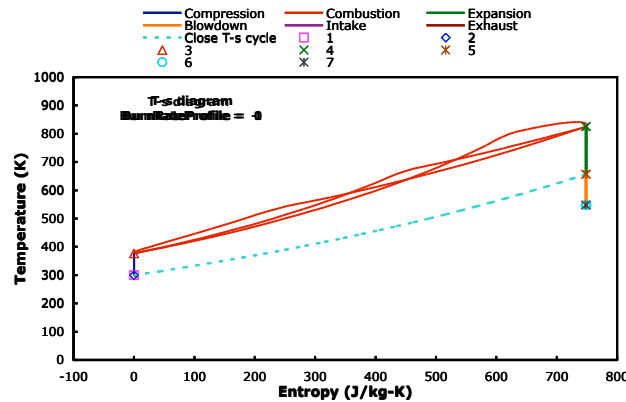
$r = 3$, $\gamma = 1.3$, $f = 0.01$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm
BurnStart = 0.1, BurnEnd = 0.1, ExhRes = FALSE, Const-v comb = TRUE
ComplExp = FALSE, $h = 0$, $T_{wall} = 400$ K, $\eta_{comp} = \eta_{exp} = 1$

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Burn Rate Profile

- Very little effect on T-s diagram - same minimum volume reached at different points in cycle
- Very little effect on efficiency - 0.244 (BurnRateProfile = 1) vs. 0.241 (BurnRateProfile = -1) for this example



$r = 3$, $\gamma = 1.3$, $f = 0.01$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm
 BurnStart = 0.2, BurnEnd = 0.2, ExhRes = FALSE, Const-v comb = TRUE
 ComplExp = FALSE, $h = 0$, $T_{wall} = 400$ K, $\eta_{comp} = \eta_{exp} = 1$

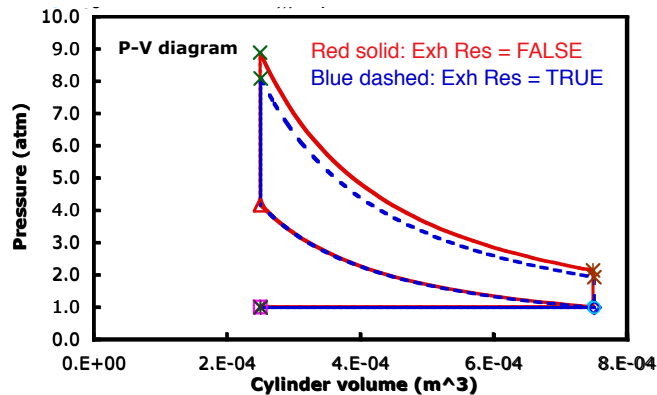
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Exhaust residual

- P-V diagram very similar, $P_2 - P_3$ is same (but gas going through cycle has higher T)
- Peak P decreases since starting at higher T_2

$$P_4/P_3 = T_4/T_3 = (T_3 + fQ_R/C_v)/T_3 = 1 + fQ_R/C_v T_3 = 1 + fQ_R/C_v T_2 \gamma^{-1}$$



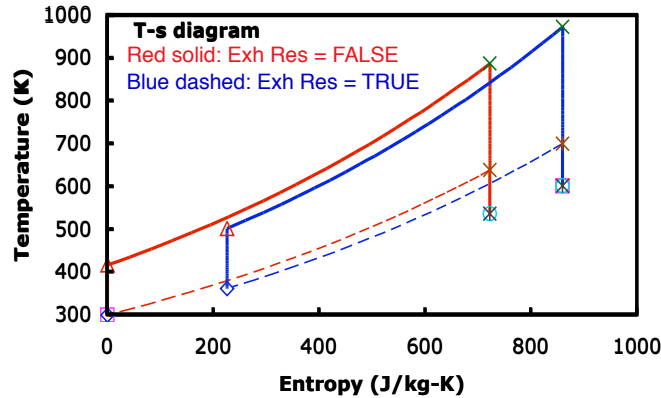
$r = 3$, $\gamma = 1.3$, $f = 0.01$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm
 ExhRes = FALSE, Const-v comb = TRUE, BurnStart = 0 or 0.05, BurnEnd = 0
 BurnRateProfile = 0, ComplExp = FALSE, $h = 0$, $T_{wall} = 400$ K, $\eta_{comp} = \eta_{exp} = 1$

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Exhaust residual

- Higher starting T & s, otherwise ideal cycle
- In ideal cycle residual has no effect on η_{th} but since exhaust residual has no fuel & lower density (higher v) than fresh gas, power or BMEP is decreased (1.84 atm vs. 2.20 atm for case shown)



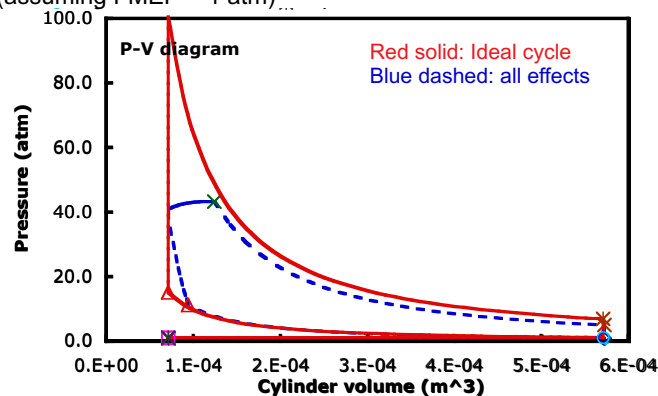
$r = 3$, $\gamma = 1.3$, $f = 0.01$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm
ExhRes = FALSE, Const-v comb = TRUE, BurnStart = 0 or 0.05, BurnEnd = 0
BurnRateProfile = 0, ComplExp = FALSE, $h = 0$, $T_{wall} = 400$ K, $\eta_{comp} = \eta_{exp} = 1$

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Complete cycle, all effects included

- Comparison of cycles with "realistic" operating parameters
- No throttling in this example
- "Spark timing" used provides maximum η_{th} for burn duration of 0.15
- Much lower peak P (less than 1/2) for non-ideal cycle
- Cycle efficiency: 0.464 vs. 0.293, IMEP 18.9 atm vs. 11.8 atm; BMEP 18.9 atm vs. 10.8 atm (assuming FMPE = 1 atm)...



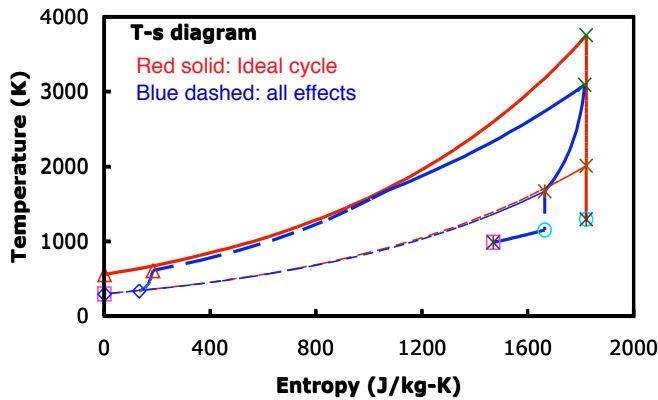
$r = 8$, $\gamma = 1.3$, $f = 0.068$, $Q_R = 4.5 \times 10^7$ J/kg, $T_{in} = 300$ K, $P_{in} = 1$ atm, $P_{exh} = 1$ atm, Const-v comb = TRUE
BurnStart = 0 or 0.045, BurnEnd = 0 or 0.105, $h = 0$ or 0.01, $T_{wall} = 400$ K, $\eta_{comp} = \eta_{exp} = 0.9$ or 1

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Complete cycle, all effects included

- Cycle starts at higher T & s due to exhaust residual + heating during intake
- s increases during compression - irreversible and non-adiabatic
- Combustion not at constant V, but eventually hits (almost) same v (slightly lower since not as much mass, thus lower v for same V)
- Less ΔT in combustion and lower peak T due to heat loss & combustion not at constant volume



Just coincidence that maximum s is same for both cycles

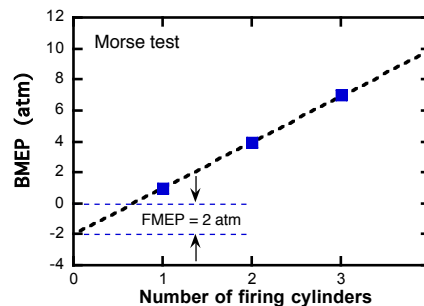
$r = 8$, $\gamma = 1.3$, $f = 0.068$, $Q_R = 4.5 \times 10^7 \text{ J/kg}$, $T_{in} = 300\text{K}$, $P_{in} = 1 \text{ atm}$, $P_{exh} = 1 \text{ atm}$, Const-v comb = TRUE
BurnStart = 0 or 0.045, BurnEnd = 0 or 0.105, $h = 0$ or 0.01, $T_{wall} = 400\text{K}$, $\eta_{comp} = \eta_{exp} = 0.9$ or 1

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Friction

- Does NOT appear on P-V or T-s diagram
- How to measure?
 - FMEP = IMEP - BMEP: measure IMEP (from P-V diagram) and BMEP (from engine work output to dynamometer); not very accurate since it's the difference between two nearly equal noisy numbers (e.g. 10 vs. 9 atm)
 - Motoring test: spin engine with electric motor, measure power needed - but firing engine has different forces/stresses, not so accurate either
 - Morse test: Remove spark plug wires one at a time, measure BMEP vs. number of firing cylinders, extrapolate to zero firing cylinders, this corresponds to IMEP = 0, BMEP will be < 0 , thus BMEP = -FMEP

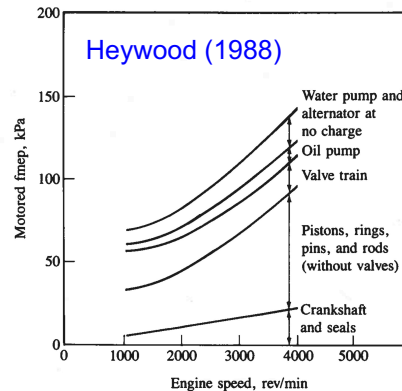


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Friction

- Typical result: FMEP increases roughly as $N^{1/2}$; since friction power = $FMEP \cdot N \cdot V_d / n$, friction power $\sim N^{1.5}$, thus at higher N , a higher % of IMEP is lost to friction (see Heywood Fig. 13-6 - 13-13)
- Typical values for automotive-size engines: $FMEP \approx 1$ atm at $N = 500$ RPM, increasing to 2.5 atm at $N = 5000$ RPM
- Not strongly dependent on IMEP (i.e. P_{intake}) for given N



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Factors that limit RPM (thus power)

- Mechanical strength of parts (obviously...)
- Choking at valves - as N increases, mass flow (\dot{m}) needed to fill cylinder increases, but for fixed intake valve area A^* , upstream pressure P_t and temperature T_t , maximum \dot{m} limited to (see Lecture 12)

$$\dot{m} = A^* \frac{P_t}{\sqrt{RT_t}} \sqrt{\gamma} \left(\frac{\gamma + 1}{2} \right)^{-(\gamma + 1)/2(\gamma - 1)}$$

With \dot{m} limited, the pressure of gas that actually gets into the cylinder (P_{cyl}) is limited:

$$\dot{m} = \rho_{cyl} V_d N / n = \frac{P_{cyl}}{RT_{cyl}} \frac{V_d N}{n} \Rightarrow P_{cyl} = \dot{m} \frac{RT_{cyl} n}{V_d N}$$

Since $IMEP \sim P_{cyl}$, once this choking occurs, as N increases further, P_{cyl} and $IMEP$ decrease

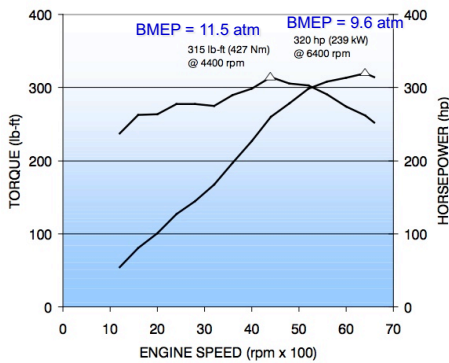
- Also - as N increases, $FMEP$ increases, $IMEP$ decreases, so $BMEP = IMEP - FMEP$ decreases drastically
- Result: Torque = $BMEP \cdot V_d / 2\pi n$ peaks at low N , power peaks at high N

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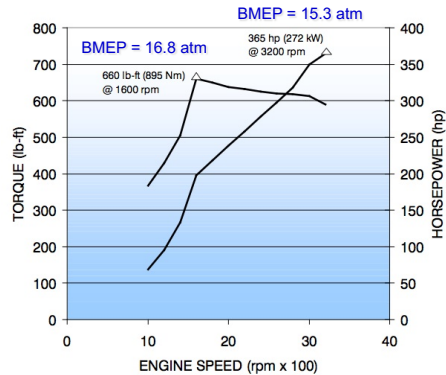
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GM truck engines - gasoline vs. Diesel

- Power (hp) = Torque (ft lb) x N (rev/min) ÷ 5252
- Gasoline: Torque ≈ constant from 1000 to 6000 RPM; power ~ N
- Turbo Diesel: Torque sharply peaked; much narrower range of usable N (1000 - 3000 RPM) (P_{intake} not reported but max. ≈ 2.3 atm from other sources)
- **Smaller, non-turbocharged gasoline engine produces almost as much power as turbo Diesel, largely due to higher N**



2010 GM Northstar 4.6 Liter V8 (LH2);
 $r = 10.5$; variable valve timing

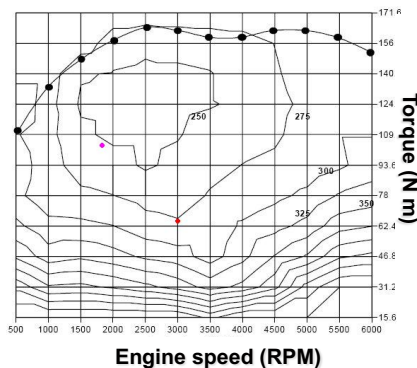


2010 GM Duramax 6.6 liter V8
turbocharged Diesel (LMM); $r = 16.8$

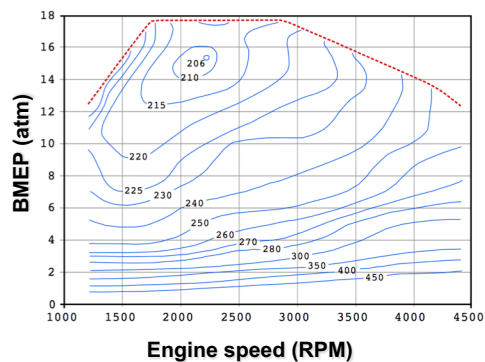
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Engine fuel consumption maps



4 cylinder, 1.9 liter gasoline (Saturn)



3 cylinder, 1.5 liter turbo Diesel

- Fuel consumption maps in units of g/kW-hr (Max $\eta_{\text{th}} \approx 40.6\%$ Diesel)
- $\text{BMEP} = 4\pi(\text{Torque})/V_d$; Max. BMEP for gasoline engine shown ≈ 10.4 atm)
- Gasoline: torque controlled by throttling; Diesel: BMEP controlled by fuel flow
- Top curve = wide open throttle (gasoline) or max. ϕ without major sooting (Diesel)
- Max Diesel efficiency $\approx 25\%$ higher than max. gasoline efficiency
- Best efficiency at lower RPM - less FMEP
- For fixed RPM, best efficiency at high load - less throttling loss (gasoline), IMEP higher relative to FMEP (both)

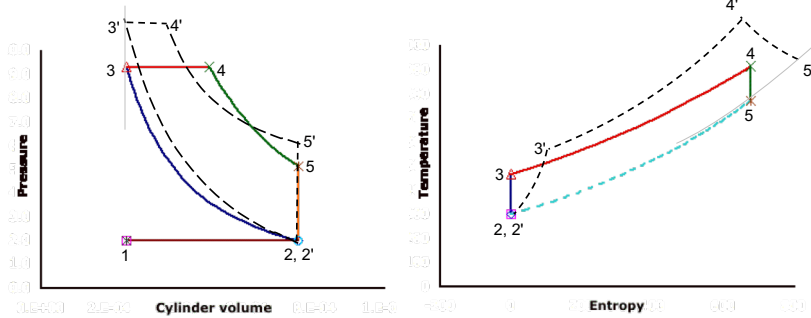
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Examples - P-V & T-s diagrams

For the ideal Diesel cycle, sketch modified P-V & T-s diagrams if the following changes are made. The initial T & P, r, f, Q_R etc. are unchanged unless otherwise stated.

- (a) The cooling system fails so that the cylinder wall temperature becomes very high and there is heat transfer from the wall to the gas throughout the cycle



Heat transfer results in higher T & P during compression, with more total heat addition. During expansion P drops more slowly than an adiabatic curve. Due to heat addition T_3, T_4, T_5 is higher than in the original cycle.

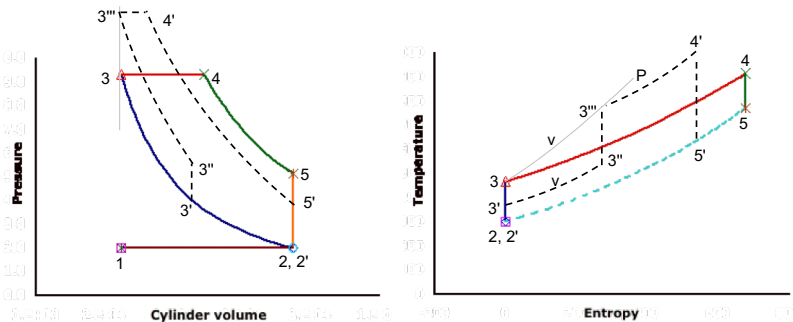
$$T_4 = T_3 + \frac{fQ_R}{C_p} \Rightarrow \frac{T_4}{T_3} = 1 + \frac{fQ_R}{C_p T_3} \text{ so as } T_3 \text{ increases, } \frac{T_4}{T_3} = \frac{V_4}{V_3} = \beta \text{ decreases}$$

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Examples - P-V & T-s diagrams

- (b) The fuel injector malfunctions and injects half of the fuel half way through the compression stroke; this part of the fuel burns instantaneously but the other half is still injected at the minimum cylinder volume and burns at constant P.



Constant V (partial) combustion then compression will result in higher T_3 & P_3 . Total heat release is the same, so areas under T-s are the same. Since T_3'' is higher and fQ_R is lower for the constant-P part of the burn, β decreases:

$$\beta' = \frac{T_4'}{T_3''} = \frac{T_3' + fQ_R(0.5)/C_p}{T_3''} = 1 + \frac{fQ_R(0.5)}{C_p T_3''}$$

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Example - numerical

For an Otto cycle with $r = 9$, $\gamma = 1.3$, $M = 0.029$ kg/mole, $f = 0.062$, $Q_R = 4.3 \times 10^7$ J/kg, $T_2 = 300$ K, $P_2 = P_{in} = 0.5$ atm, $P_6 = P_{ex} = 1$ atm, $h = 0$, $\eta_{comp} = \eta_{exp} = 0.9$, determine the following:

- a) T & P after compression and compression work per kg of mixture

$$\eta_{comp} = \frac{\left(\frac{v_2}{v_3}\right)^{\gamma-1} - 1}{\left(\frac{T_3}{T_2}\right) - 1}; \frac{v_2}{v_3} = \frac{V_2/m}{V_3/m} = \frac{V_2}{V_3} = r = 9; \eta_{comp} = 0.9 = \frac{(9)^{0.3} - 1}{\left(\frac{T_3}{T_2}\right) - 1} \Rightarrow \frac{T_3}{T_2} - 1 = 1.037 \Rightarrow T_3 = 611 \text{ K}$$

$$P_2 v_2 = RT_2, P_3 v_3 = RT_3 \Rightarrow P_3 = \frac{v_2}{v_3} \frac{T_3}{T_2} P_2 = 9 \frac{611 \text{ K}}{300 \text{ K}} (0.5 \text{ atm}) = 9.165 \text{ atm}$$

$$\frac{\text{Work}}{\text{mass}} = -C_v(T_3 - T_2); C_v = \frac{R}{\gamma - 1} = \frac{\mathfrak{R}/M}{\gamma - 1} = \frac{8.314 \text{ J/moleK}}{1.3 - 1} = \frac{955.6 \text{ J}}{\text{kgK}}$$

$$\frac{\text{Work}}{\text{mass}} = -\frac{955.6 \text{ J}}{\text{kgK}} (611 \text{ K} - 300 \text{ K}) = -2.97 \times 10^5 \frac{\text{J}}{\text{kg}}$$

- b) Temperature (T_4) and pressure (P_4) after combustion

$$T_4 = T_3 + \frac{fQ_R}{C_v} = 611 \text{ K} + \frac{(0.062)(4.3 \times 10^7 \text{ J/kg})}{955.6 \text{ J/kgK}} = 3401 \text{ K};$$

$$PV = mRT \Rightarrow \frac{P_4 V_4}{P_3 V_3} = \frac{mRT_4}{mRT_3} \Rightarrow P_4 = \frac{T_4}{T_3} P_3 = \frac{3401 \text{ K}}{611 \text{ K}} 9.165 \text{ atm} \Rightarrow P_4 = 51.02 \text{ atm}$$

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Example - numerical - continued

- c) Temperature (T_5) and pressure (P_5) after expansion, and the expansion work per kg of mixture

$$\eta_{exp} = \frac{\frac{T_5}{T_4} - 1}{\left(\frac{v_4}{v_5}\right)^{\gamma-1} - 1} \Rightarrow 0.9 \left[\left(\frac{1}{9}\right)^{1.3-1} - 1 \right] = \frac{T_5}{3401 \text{ K}} - 1 \Rightarrow T_5 = 1923 \text{ K};$$

$$\frac{P_4 V_4}{P_5 V_5} = \frac{T_4}{T_5} \Rightarrow \frac{51.02 \text{ atm} \left(\frac{1}{9}\right)}{P_5} = \frac{3401 \text{ K}}{1923 \text{ K}} \Rightarrow P_5 = 3.205 \text{ atm}$$

$$\frac{\text{Expansion work}}{\text{mass}} = -C_v \Delta T = -\frac{955.6 \text{ J}}{\text{kgK}} (1923 \text{ K} - 3401 \text{ K}) = 1.412 \times 10^6 \text{ J/kg}$$

- d) Net work per kg of mixture (don't forget about the throttling loss!)

$$\frac{\text{Pumping work}}{\text{mass}} = \frac{(P_{in} - P_{ex})V_d}{(P_{in}V_d)/RT} = RT \left(1 - \frac{P_{ex}}{P_{in}}\right) = \frac{8.314 \text{ J/moleK}}{0.029 \text{ kg/mole}} 300 \text{ K} \left(1 - \frac{1 \text{ atm}}{0.5 \text{ atm}}\right) = -8.60 \times 10^4 \frac{\text{J}}{\text{kg}}$$

Net work = compression work + expansion work + pumping work

$$\text{Net work/mass} = -2.97 \times 10^5 + 1.412 \times 10^6 - 8.60 \times 10^4 = 1.029 \times 10^6 \frac{\text{J}}{\text{kg}}$$

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Example - numerical - concluded

e) Thermal efficiency

$$\eta_{th} = \frac{\text{Net Work}}{\text{Heat Input}} = \frac{\text{Work/mass}}{fQ_R} = \frac{1.029 \times 10^6 \text{ J/kg}}{(0.062)(4.3 \times 10^7 \text{ J/kg})} = 0.386 = 38.6\%$$

$$\eta_{th}(\text{ideal}) = 1 - \frac{1}{r^{\gamma-1}} = 1 - \frac{1}{9^{1.3-1}} = 0.483 = 48.3\% > 38.6\% \text{ (passes reality check)}$$

f) IMEP

$$\begin{aligned} \text{IMEP} &= \frac{\text{Net Work}}{V_d} = \frac{\text{Net work/mass}}{V_d/\text{mass}} = \frac{\text{Net work/mass}}{V_d/(V_d/\rho_2)} = \rho_2(\text{Net work/mass}) \\ &= (\text{Net work/mass}) \left(\frac{P_2}{(\mathcal{R}/M)T_2} \right) = \frac{0.5 \text{ atm}}{\frac{8.314 \text{ J/moleK}}{0.029 \text{ kg/mole}} (300 \text{ K})} \left(1.029 \times 10^6 \frac{\text{J}}{\text{kg}} \right) = 5.98 \text{ atm} \end{aligned}$$

f) Temperature of exhaust gas after blowdown

$T_5 = 1923 \text{ K}, P_5 = 3.205 \text{ atm}$. Assuming blowdown is isentropic to 1 atm:

$$\frac{T_6}{T_5} = \left(\frac{P_6}{P_5} \right)^{\frac{\gamma-1}{\gamma}} \Rightarrow T_6 = T_5 \left(\frac{P_6}{P_5} \right)^{\frac{\gamma-1}{\gamma}} = 1923 \text{ K} \left(\frac{1 \text{ atm}}{3.205 \text{ atm}} \right)^{1.3-1/1.3} = 1470 \text{ K}$$

Summary

- "Real" cycles differ from ideal cycles in ways that significantly affect performance predictions
 - Irreversible compression/expansion lowers η
 - » More ΔT (thus more work) during compression
 - » Less ΔT (thus less work) during expansion
 - Heat transfer to gas during cycle - sounds good, but it takes more work to compress a hot gas than a cold gas, lowers η !
 - Finite burn time
 - » Best η when burning occurs at min. v or max. $P \Rightarrow$ max. T
 - Exhaust residual - hot exhaust gas mixing with fresh intake gas decreases ρ (increases specific volume $v = 1/\rho$) decreasing power (though not necessarily η)
 - Friction – doesn't affect states of gas, but affects net Power & η
- Since engines are essentially air processors, any factor that limits air flow limits power